

2023

6th Semester Examination

PHYSICS (Honours)

Paper : C 14-T

[Statistical Mechanics]

[CBCS]

Full Marks : 40

Time : Two Hours

*The figures in the margin indicate full marks.
Candidates are required to give their answers
in their own words as far as practicable.*

Group - A

Answer any **five** questions : $2 \times 5 = 10$

1. Show that electron gas in a white dwarf star is strongly degenerate and relativistic in nature. 2
2. Write statistical definition of temperature in terms of accessible microstates. Assuming the number of accessible microstates $\Omega(E, V) \propto \left(V^N E^{\frac{3N}{2}} \right)$, find the molar specific heat at constant volume. 2
3. Which among the Bose-Einstein and Fermi-Dirac statistics will be followed by (i) Neutrons, (ii) Alpha particles, (iii) Deuterium nuclei, and (iv) ${}^3_2\text{He}$ atoms? 2

P.T.O.

(3)

where a and n are constants, g_s is spin degeneracy and V is the volume. Calculate the Fermi energy and total energy of the system at zero Kelvin temperature. 5

13. The specific heat of a metal (in three dimensions) at low temperatures can be represented by $C_V = aT + bT^3$, where a and b are constants. Explain the origin of the first term with necessary deduction. 5
14. Starting from Planck's law deduce (i) Rayleigh-Jeans law and (ii) Wien's law. $2\frac{1}{2}+2\frac{1}{2}$

Group - C

Answer any *one* question : $10 \times 1 = 10$

15. (a) Calculate deviation of an ideal Fermi gas equation from the perfect gas equation for weak degeneracy. How is it related to gas degeneracy? 5+2
- (b) An atom has a non-degenerate ground state with energy $\epsilon_0 = 0$ and a doubly degenerate excited state with energy $\epsilon_1 = \epsilon$. Calculate the specific heat at very low temperature ($\beta\epsilon \gg 1$). 3
16. Write down the single particle partition function for a system having two non-degenerate energy levels with energies : $\epsilon_1 = -\mu H$ and $\epsilon_2 = \mu H$. Evaluate entropy for this system. Hence discuss the concept of negative absolute temperature of such a two-level system. $4+4+2$

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